

# Horizontal Forces

### Sample 1

The amazing water skiing gazelle (mass = 60 kg) can ski behind a boat (mass = 1000 kg) when the engine provides 5000 N of force. The maximum tension of the ski rope is 400 N. What is the maximum acceleration of the gazelle.

**Draw the FBD for the Gazelle**

**Write the Net Force Equations (both X and Y)**

$\Sigma F_x :$	$T = ma$
$\Sigma F_y :$	$F_N - F_g = ma \rightarrow 0$

**CHOOSE THE NET FORCE EQUATIONS THAT ARE RELEVANT TO THIS PROBLEM (in this case they are the x net force equations)**

$\Sigma F_x :$	$400 \text{ N} = (60\text{kg}) a$
	$a = 6.67 \text{ m/s}^2$

### Sample 2

The amazing water skiing gazelle (mass = 60 kg) is again skiing behind a boat (mass = 1000 kg) when the engine provides 5000 N of force. What is the acceleration of the gazelle and the boat? What is the tension in the rope between the gazelle and the boat?

**Draw the FBD's for the Gazelle and the boat**

**Write net force equations (X and Y) for the gazelle and the boat**

$\Sigma F_x :$	$T = ma$	$\Sigma F_x :$	$F_{eng} - T = ma$
$\Sigma F_y :$	$F_N - F_g = ma \rightarrow 0$	$\Sigma F_y :$	$F_N - F_g = ma \rightarrow 0$
$\Sigma F_x :$	$T = (60 \text{ kg})a$	$\Sigma F_x :$	$5000 \text{ N} - T = (1000 \text{ kg})a$
$\Sigma F_y :$	$F_N - (60 \text{ kg})(9.8 \text{ m/s}^2) = 0 \text{ N}$	$\Sigma F_y :$	$F_N - (1000 \text{ kg})(9.8 \text{ m/s}^2) = 0 \text{ N}$

**CHOOSE THE NET FORCE EQUATIONS THAT ARE RELEVANT (in this case they are the x net force equations)**

$\Sigma F_x :$	$T = (60 \text{ kg})a$	$\Sigma F_x :$	$5000 \text{ N} - T = (1000 \text{ kg})a$
----------------	------------------------	----------------	---

**SUBSTITUTE ONE EQUATION INTO THE OTHER TO SOLVE FOR a**

$$5000 \text{ N} - (60 \text{ kg})a = (1000 \text{ kg})a$$

$$5000 \text{ N} = (1060 \text{ kg})a$$

$$a = 4.72 \text{ m/s}^2$$

**Plug a into the one of the original equations and solve for T**

$$T = (60 \text{ kg})a$$

$$T = (60 \text{ kg})(4.72 \text{ m/s}^2)$$

$$T = 283 \text{ N}$$

# Vertical Forces

## Sample 1

Star Flight, in an attempt to rescue an injured gazelle, lowers a cable which can withstand a maximum tension of 800 N to the 60 kg gazelle trapped at the bottom of a canyon. What is the maximum acceleration that Star Flight can use to lift the gazelle?

**Draw the FBD for the Gazelle**

**Write the Net Force Equation**

$$\Sigma F_y : T - F_g = ma$$

$$\Sigma F_y : 800 \text{ N} - (60 \text{ kg})(9.8 \text{ m/s}^2) = (60 \text{ kg})a$$

$$a = 3.53 \text{ m/s}^2$$

## Sample 2

Two hanging plants are suspended from the ceiling of an elevator as shown in the picture. What are the tensions in the two cables if the elevator is accelerating **downward** at 3 m/s<sup>2</sup>?

**Draw the FBD's**

**Write net force equations (Y) for both objects**

**NOTE: you MUST use a NEGATIVE sign with the acceleration because the elevator is going down!!!!**

$$\Sigma F_y : T_1 - T_2 - F_g = ma$$

$$\Sigma F_y : T_1 - T_2 - (6 \text{ kg})(9.8 \text{ m/s}^2) = (6 \text{ kg})(-3 \text{ m/s}^2)$$

$$\Sigma F_y : T_2 - F_g = ma$$

$$\Sigma F_y : T_2 - (4.5 \text{ kg})(9.8 \text{ m/s}^2) = (4.5 \text{ kg})(-3 \text{ m/s}^2)$$

**Solve for T<sub>2</sub>**

$$\Sigma F_y : T_2 - (4.5 \text{ kg})(9.8 \text{ m/s}^2) = (4.5 \text{ kg})(-3 \text{ m/s}^2)$$

$$T_2 = 30.6 \text{ N}$$

**Substitute and solve for T<sub>1</sub>**

$$\Sigma F_y : T_1 - 30.6 \text{ N} - (6 \text{ kg})(9.8 \text{ m/s}^2) = (6 \text{ kg})(-3 \text{ m/s}^2)$$

$$T_1 = 71.4 \text{ N}$$

## Review for Unit 4

Terms to know:

- Force
- Contact Force
- Field Force
- Inertia
- Acceleration
- Mass
- Weight ( $F_g$ )
- Action-reaction forces

### • Concepts to Know:

- Know Newton's three laws of motion
  - Law of Inertia
  - Law of Acceleration (and its mathematical representation)
  - Law of Interactions
- Know what a force is and what it does to an object
- Know the two types of forces, be able to describe the differences and classify examples as either field or contact forces
- Understand the relationship between force, mass and acceleration

- Be able to:
  - Draw and label free-body diagrams and determine net force
  - Calculate the net force
  - Calculate force, mass, weight and acceleration
  - Determine net force:  $\Sigma F = ma$
  - Weight/Force gravity:  $F_g = mg$  ( $g = +9.8 \text{ m/s}^2$ )
  - Write net force equations
- There will be multiple choice questions as well as force problems.