

1. A 20 kg board serves as a seesaw for two children, as shown in the figure. One child has a mass of 30 kg and sits 2.5 m from the pivot point. a.) Calculate the force the fulcrum must provide. b.) At what distance,  $x$ , from the pivot must a 25 kg child place herself to balance the seesaw? Assume the board is centered over the pivot.

FBD:

$F = (30)(9.8) = 294 \text{ N}$   
 $F = (20)(9.8) = 196 \text{ N}$   
 $F = (25)(9.8) = 245 \text{ N}$

$\Sigma F_y: F_{ful} - (30)(9.8) - (20)(9.8) - (25)(9.8) = 0$   
 $F_{ful} = 735 \text{ N}$

$\Sigma \tau: (294)(2.5) - (245)(x) = 0$   
 $x = \frac{(294)(2.5)}{245} = 3 \text{ m}$

$F = 735 \text{ N}$   
 $x = 3 \text{ m}$

2. A uniform 1500 kg beam, 20.0 m long, supports 15,000 kg of bricks. Calculate the force on each of the supports.

FBD:

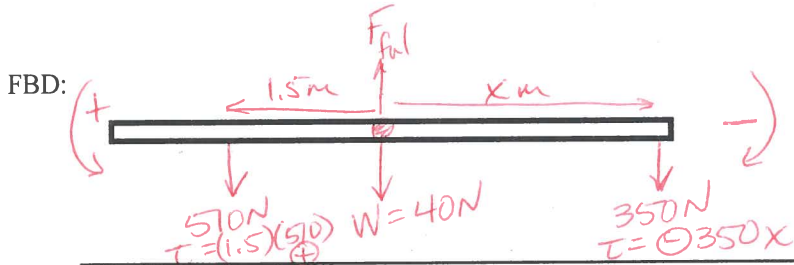
$F_1$  at left support,  $F_2$  at right support  
 Beam weight  $F = (1500)(9.8) = 14,700 \text{ N}$  at 10 m from left support  
 Brick weight  $F = (15,000)(9.8) = 147,000 \text{ N}$  at 17 m from left support

$\Sigma F_y: F_1 + F_2 - 14,700 - 147,000 = 0$   
 $F_1 + 132,300 - 14,700 - 147,000 = 0$

$\Sigma \tau: 20 F_2 - (14,700)(10) - (147,000)(17) = 0$   
 $F_2 = \frac{14,700 + 2,499,000}{20} = 132,300 \text{ N}$

$F_1 = 29,400 \text{ N}$   
 $F_2 = 132,300 \text{ N}$

3. A uniform board with a weight of 40 N supports two children, one weighing 510 N and the other weighing 350 N. The support for the beam is directly under the beam's center of mass. The 510 N child is 1.5 meters from the center of the board. Where should the 350 N child sit to balance the board? How much force must the support exert on the board?



$$\Sigma F_y: F_{ful} - 510 - 40 - 350 = 0$$

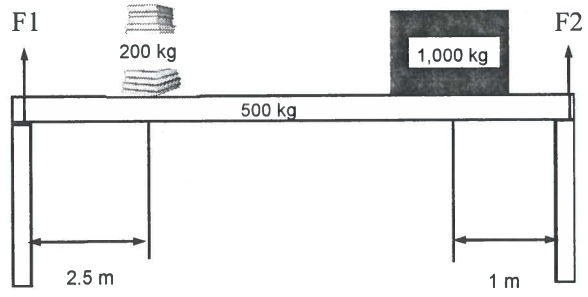
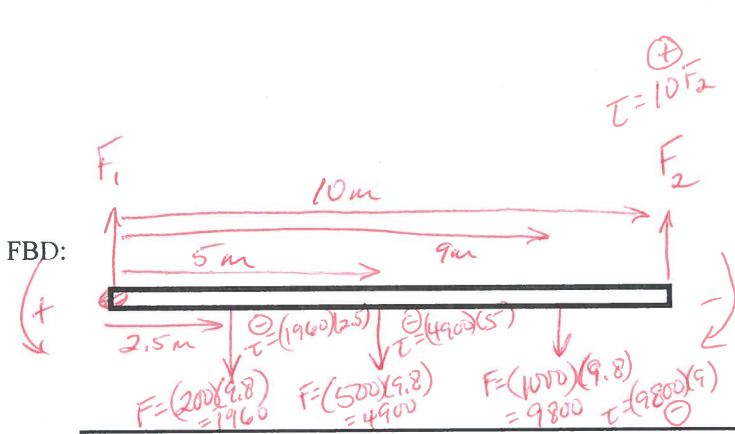
$$F_{ful} = 900 \text{ N}$$

|        |
|--------|
| 900 N  |
| 2.19 m |

$$\Sigma \tau: (1.5)(510) - 350x = 0$$

$$\frac{350x}{350} = \frac{765}{350} = 2.19 \text{ m}$$

4. A uniform 500 kg beam, 10.0 m long, supports 1,000 kg of bricks and a 200 kg stack of reference books about gazelles. Calculate the force on each of the supports.



$$\Sigma F_y: F_1 + F_2 - 1960 - 4900 - 9800 = 0$$

$$F_1 = 1960 + 4900 + 9800 - 11,760$$

|                          |
|--------------------------|
| $F_1 = 4,900 \text{ N}$  |
| $F_2 = 11,760 \text{ N}$ |

$$\Sigma \tau: 10 F_2 - (1960)(2.5) - (4900)(5) - (9800)(9) = 0$$

$$F_2 = \frac{4,900 + 24,500 + 88,200}{10} = 11,760 \text{ N}$$